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Vectors and More

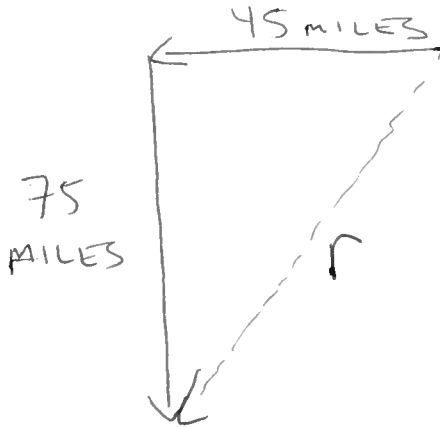
$d = vt$

$v_f = v_i + at$

$d = v_i t + (1/2)at^2$

$g = 9.8 \text{ m/s}^2$

- 1) A person travels 45 miles to the west. They then travel 75 miles to the south. Draw a head to tail diagram for this scenario. Calculate the person's resultant displacement. In other words, calculate how far they are from their starting point.



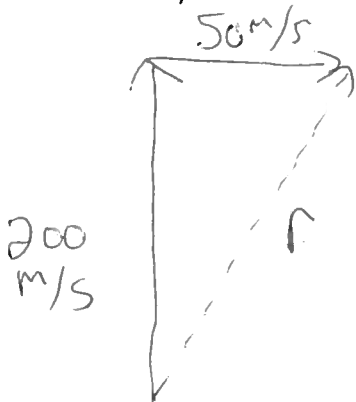
$r^2 = 45^2 + 75^2$

$r^2 = 7650$

$r = \sqrt{7650}$

$r = \boxed{87.5 \text{ MILES}}$

- 2) A plane heads to the north at 200 m/s but a wind pushes it to the east at 50 m/s.
- What is the resultant velocity of the plane?
 - How far does the plane travel in 2 hours?



a) $r^2 = 50^2 + 200^2$

$r^2 = 42500$

$r = \sqrt{42500}$

$r = 206 \text{ m/s}$

b) $v = 206 \frac{\text{m}}{\text{s}}$

$t = 2 \text{ hours} \times \frac{60 \text{ min}}{\text{hr}} \times \frac{60 \text{ s}}{\text{min}} = 7200 \text{ s}$

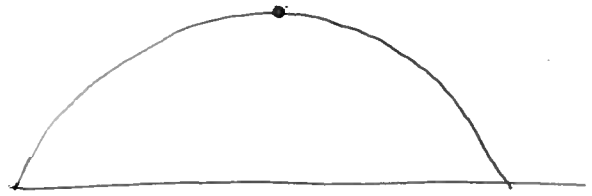
$d = vt$

$d = (206)(7200) = \boxed{1,483,200 \text{ m}}$

$$d = vt \quad v_f = v_i + at \quad d = v_i t + (1/2)at^2 \quad g = 9.8 \text{ m/s}^2$$

3) A projectile is fired from the ground at an angle. The velocity of the projectile is initially 30 m/s in the horizontal direction and 60 m/s in the vertical direction.

- What is the hang time for the projectile?
- What is the maximum height for the projectile?
- What is the range of the projectile?



$$\begin{array}{l} \underline{X} \\ v = 30 \text{ m/s} \\ t = 12.2 \text{ s} \end{array}$$

$$\begin{array}{l} c) d = vt \\ d = (30)(12.2) \\ d = \boxed{366 \text{ m}} \end{array}$$

$$\begin{array}{l} \underline{Y \text{ ON THE WAY DOWN}} \\ v_i = 0 \frac{\text{m}}{\text{s}} \\ a = 9.8 \text{ m/s}^2 \\ v_f = 60 \frac{\text{m}}{\text{s}} \end{array}$$

$$\begin{array}{l} v_f = v_i + at \\ 60 = v_i + (9.8)t \\ \frac{60}{9.8} = t = 6.1 \text{ s} \end{array}$$

$$a) \text{ HANG TIME} = 6.1 \times 2 = \boxed{12.2 \text{ s}}$$

$$\begin{array}{l} b) d = v_i t + \frac{1}{2} a t^2 \\ d = \frac{1}{2} (9.8) t^2 \\ d = 4.9 t^2 \\ d = 4.9 (6.1)^2 \\ d = \boxed{182 \text{ m}} \end{array}$$

$$d = vt \quad v_f = v_i + at \quad d = v_i t + (1/2)at^2 \quad g = 9.8 \text{ m/s}^2$$

- 4) A car travels at a constant speed for 7 seconds. The car then accelerates at 4 m/s^2 for 5 seconds. During the 5 seconds of acceleration, the car travels 200 m. How far does the car travel all together?

PART 1

$$t = 7 \text{ s}$$

$$v = 30 \text{ m/s}$$

$$d = vt$$

$$d = (30)(7)$$

$$d = \underline{\underline{210 \text{ m}}}$$

PART 2

$$a = 4 \text{ m/s}^2$$

$$t = 5 \text{ s}$$

$$d = 200 \text{ m}$$

$$d = v_i t + \frac{1}{2} a t^2$$

$$200 = v_i(5) + \frac{1}{2}(4)(5)^2$$

$$200 = v_i(5) + 50$$

$$150 = v_i(5)$$

$$\frac{150}{5} = v_i = \underline{\underline{30 \text{ m/s}}}$$

$$\underline{\underline{\text{TOTAL DISTANCE}}} = 210$$

$$+ 200$$

$$\boxed{410 \text{ m}}$$