

Name SOLUTIONS

Date

106

## Mechanical Energy Practice

$$PE = mgh \quad KE = \frac{1}{2} mv^2$$

1) A 25 kg object is held at 3 m above the ground. What is its potential energy?

$$m = 25 \text{ kg}$$

$$h = 3 \text{ m}$$

$$PE = ?$$

$$PE = mgh$$

$$PE = (25)(9.8)(3)$$

$$PE = \boxed{735 \text{ J}}$$

2) A 100 kg object has a potential energy of 14,700 J. How high off the ground is it?

$$m = 100 \text{ kg}$$

$$PE = 14,700 \text{ J}$$

$$h = ?$$

$$PE = mgh$$

$$14700 = (100)(9.8)h$$

$$14700 = 980h$$

$$\frac{14700}{980} = h = \boxed{15 \text{ m}}$$

3) An object has a potential energy of 1000 J. The object is 5 m off the ground. What is its mass?

$$PE = 1000 \text{ J}$$

$$h = 5 \text{ m}$$

$$m = ?$$

$$PE = mgh$$

$$1000 = m(9.8)(5)$$

$$1000 = m(49)$$

$$\frac{1000}{49} = m = \boxed{20.4 \text{ kg}}$$

4) A 20 kg mass is moving at 10 m/s. What is its kinetic energy?

$$m = 20 \text{ kg}$$

$$v = 10 \frac{\text{m}}{\text{s}}$$

$$KE = ?$$

$$KE = \frac{1}{2} mv^2$$

$$KE = \frac{1}{2} (20)(10)^2$$

$$KE = (10)(100)$$

$$KE = \boxed{1000 \text{ J}}$$

Answers: 1) 735 J 2) 15 m 3) 20.4 kg 4) 1000 J

5) A 25 kg mass has a kinetic energy of 1250 J. What is its speed?

$$M = 25 \text{ kg}$$

$$KE = 1250 \text{ J}$$

$$v = ?$$

$$KE = \frac{1}{2}mv^2$$

$$1250 = \frac{1}{2}(25)v^2$$

$$1250 = 12.5v^2$$

$$\frac{1250}{12.5} = v^2$$

$$\sqrt{100} = v = \boxed{10 \text{ m/s}}$$

6) An object moving at 50 m/s has a kinetic energy of 5000 J. What is its mass?

$$v = 50 \frac{\text{m}}{\text{s}}$$

$$KE = 5000 \text{ J}$$

$$m = ?$$

$$KE = \frac{1}{2}mv^2$$

$$5000 = \frac{1}{2}m(50)^2$$

$$5000 = \frac{1}{2}m(2500)$$

$$5000 = 1250m$$

$$\frac{5000}{1250} = m = \boxed{4 \text{ kg}}$$

7) A 70 kg snowboarder is at the top of a 100 m mountain. Before the snowboarder begins to move,

a) what is their potential energy?

$$M = 70 \text{ kg}$$

$$h = 100 \text{ m}$$

$$PE = ?$$

$$v = 0 \text{ m/s}$$

$$PE = mgh$$

$$PE = (70)(9.8)(100)$$

$$PE = \boxed{68,600 \text{ J}}$$

b) What is their kinetic energy?

$$KE = \frac{1}{2}mv^2$$

$$KE = \frac{1}{2}(70)(0)^2$$

$$KE = \boxed{0 \text{ J}}$$

c) What is their total energy?

$$TE = KE + PE$$

$$TE = 0 + 68,600$$

$$TE = \boxed{68,600 \text{ J}}$$

Answers: 5) 10 m/s 6) 4 kg 7a) 68600 J b) 0 J c) 68600 J

8) When the snowboarder has reached a point where they are 40 m vertically above the ground,

a) what is their potential energy?

$$m = 70 \text{ kg}$$

$$h = 40 \text{ m}$$

$$PE = ?$$

$$PE = mgh$$

$$PE = (70)(9.8)(40)$$

$$PE = \boxed{27,440 \text{ J}}$$

b) What is their total energy?

$$TE = \boxed{68,600 \text{ J}}$$

(STAYS CONSTANT THROUGHOUT)

c) What is their kinetic energy?

$$TE = KE + PE$$

$$68,600 = KE + 27,440$$

$$68,600 - 27,440 = KE$$

$$\boxed{41,160 \text{ J}} = KE$$

d) What is their speed?

$$KE = \frac{1}{2}mv^2$$

$$41,160 = \frac{1}{2}(70)v^2$$

$$41,160 = 35v^2$$

$$\sqrt{\frac{41,160}{35}} = v = \boxed{34.3 \text{ m/s}}$$

Answers: 8a) 27440 J b) 68600 J c) 41160 J d) 34.3 m/s

- 9) When the snowboarder has reached the ground,  
a) what is their potential energy?

$$m = 70 \text{ kg} \quad PE = mgh$$

$$h = 0 \text{ m} \quad PE = (70)(9.8)(0)$$

$$PE = ? \quad PE = \boxed{0 \text{ J}}$$

- b) What is their total energy?

$$TE = \boxed{68,600 \text{ J}}$$

(STAYS CONSTANT THROUGHOUT)

- c) What is their kinetic energy?

$$TE = KE + PE$$

$$68,600 = KE + 0$$

$$\boxed{68,600 \text{ J}} = KE$$

- d) What is their speed?

$$KE = \frac{1}{2} m v^2$$

$$68,600 = \frac{1}{2} (70) v^2$$

$$68,600 = 35 v^2$$

$$\sqrt{\frac{68,600}{35}} = v = \boxed{44.27 \text{ m/s}}$$

Answers: 9a) 0 J b) 68600 J c) 68600 J d) 44.27 m/s